



IB MYP Year 5
 Year 10 Mathematics
 Assessment #3



TRIGONOMETRIC PATTERNS

Unit Question: How do we get around? aTeachers: Ms. Luk & Mr. Slosberg
 End Date: March 15, 2013 Time Allowed: Double Lesson
 Concept Statement: The student will discover one or two formulas which will be useful in the future.

The objective of this task is discover a useful formula for finding out new trig. values from old ones.

IN YOUR BOOK:

- ◆ **New Trends Mathematics**, Chapter 3 & 9 on Trigonometry

INSTRUCTIONS:

- ◆ Read the **instructions** and **rubric** carefully.
- ◆ Show all **steps** and proper **units**.
- ◆ Submit **your own work**. Any copying or other cheating, will automatically receive a 0.
- ◆ You are allowed to use non-electronic **dictionary**.
- ◆ **Calculators** are allowed.

ASSESSMENT:

- ◆ Read the criteria descriptors on the next page carefully before you start your work. This will give you a clear understanding of what is required and what a quality piece of work for this task must include. This way you give yourself the best chance of achieving the highest level in this task.
- ◆ This task assesses Criteria B.

CRITERION B: INVESTIGATING PATTERNS

Achievement level	Task Specific Rubric	IBO Published Descriptor	Student's Self-Evaluation
0	The student does not reach a standard described by any of the descriptors given below.	The student does not reach a standard described by any of the descriptors given below.	(0-8)
1-2 Do Maths	The student can calculate trigonometric values correctly.	The student applies, with some guidance , mathematical problem-solving techniques to recognize simple patterns.	
3-4 General Rule	The student comes up with a general rule relating the trigonometric ratios.	The student applies mathematical problem-solving techniques to recognize patterns, and suggests relationships or general rules.	Teacher's Final Grade
5-6 Test it	The student tests their general rule by taking a few more examples.	The student selects and applies mathematical problem-solving techniques to recognize patterns, describes them as relationships or general rules, and draws conclusions consistent with findings.	
7-8 Prove it	The student explains how certain they are that they are right and why.	The student selects and applies mathematical problem-solving techniques to recognize patterns, describes them as relationships or general rules, draws the correct conclusions consistent with the correct findings, and provides justifications or proofs .	

ASSESSMENT

Level 1-2

1. Given the following expressions, evaluate

- a. $\sin(x)$
- b. $\sin(2x)$
- c. $\sin^2(x)$
- d. $\cos(x)$
- e. $\cos(2x)$
- f. $\cos^2(x)$

for $x = 30^\circ, 150^\circ, 240^\circ, 330^\circ$.

Level 3-4

- 2. Organize the data you found from question 1.
- 3. Describe a general rule you found involving either $\sin(2x)$ or $\cos(2x)$

Level 5-6

- 4. Suggest another example or two to make certain it is right.

Level 7-8

- 5. Test your pattern with other methods/identities, justify your formula(s) and give limitations if there's any.

~ End of Assessment ~



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~~sin~~

1a)

$$\sin 30^\circ$$

$$= \frac{1}{2}$$

$$\sin 150^\circ$$

$$= \frac{1}{2}$$

$$\sin 240^\circ$$

$$= -\frac{\sqrt{3}}{2}$$

$$\sin 330^\circ$$

$$= -\frac{1}{2}$$

1b)

$$\sin 30^\circ (2)$$

$$= \sin 60^\circ$$

$$= \frac{\sqrt{3}}{2}$$

$$\sin 150^\circ (2)$$

$$= \sin 300^\circ$$

$$= -\frac{\sqrt{3}}{2}$$

$$\sin 240^\circ (2)$$

$$= \sin 480^\circ$$

$$= \frac{\sqrt{3}}{2}$$

$$\sin 330^\circ (2)$$

$$= \sin 660^\circ$$

$$= -\frac{\sqrt{3}}{2}$$

$$1c) \sin^2 (30^\circ)$$

$$= 0$$

$$\sin^2 (150^\circ)$$

$$= 0$$

$$\sin^2 (240^\circ)$$

$$= 0$$

$$\sin^2 (330^\circ)$$

$$= 0$$

$$1d) \cos (30^\circ)$$

$$= \frac{\sqrt{3}}{2}$$

$$\cos (150^\circ)$$

$$= -\frac{\sqrt{3}}{2}$$

$$\cos (240^\circ)$$

$$= -\frac{1}{2}$$

$$\cos (330^\circ)$$

$$= \frac{\sqrt{3}}{2}$$

$$1e) \cos (2 \times 30^\circ)$$

$$= \cos 60^\circ$$

$$= \frac{1}{2}$$

$$\cos(2 \times 150^\circ)$$

$$= \cos 300$$

$$= \frac{1}{2}$$

$$\cos(2 \times 240^\circ)$$

$$= \cos 480^\circ$$

$$= -\frac{1}{2}$$

$$\cos(2 \times 330^\circ)$$

$$= \cos 660^\circ$$

$$= \frac{1}{2}$$

1 f)

$$\cos^2(30^\circ)$$

$$= -1$$

$$\cos^2(150^\circ)$$

$$= 0$$

$$\cos^2(240^\circ)$$

$$= 1$$

$$\cos^2(330^\circ)$$

$$= -1$$



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		$\sin(x)$	$\sin(2x)$	$\sin^2(x)$	$\cos(x)$	$\cos(2x)$	$\cos^2(x)$
2)	30°	$\frac{1}{2}$	$\frac{\sqrt{3}}{2} (60^\circ)$	0	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$-1 (60^\circ)$
	150°	$\frac{1}{2}$	$-\frac{\sqrt{3}}{2} (300^\circ)$	0	$-\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$0 (300^\circ)$
	240°	$-\frac{\sqrt{3}}{2}$	$\frac{\sqrt{3}}{2} (480^\circ)$	0	$-\frac{1}{2}$	$-\frac{1}{2}$	$1 (480^\circ)$
	330°	$-\frac{1}{2}$	$-\frac{\sqrt{3}}{2} (660^\circ)$	0	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$-1 (660^\circ)$

3) Describe a general rule you found involving either $\sin(2x)$ or $\cos(2x)$:

The general rule I found involving $\sin(2x)$ was $\frac{\sqrt{3}}{2}, -\frac{\sqrt{3}}{2}, \frac{\sqrt{3}}{2}$ and $-\frac{\sqrt{3}}{2}$.

Suggest another example or two to make certain it is right.

4) $\cos(420^\circ)(2)$

$$= \cos 840$$

$$= -\frac{1}{2}$$

5)